

# Production of Hypernuclei

H. Lenske



**Institut für  
Theoretische Physik**



# Topics:

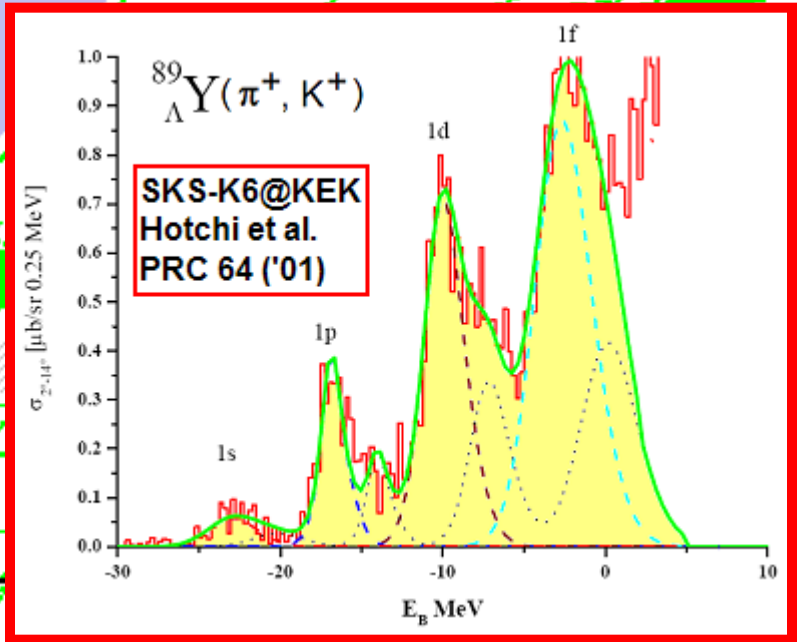
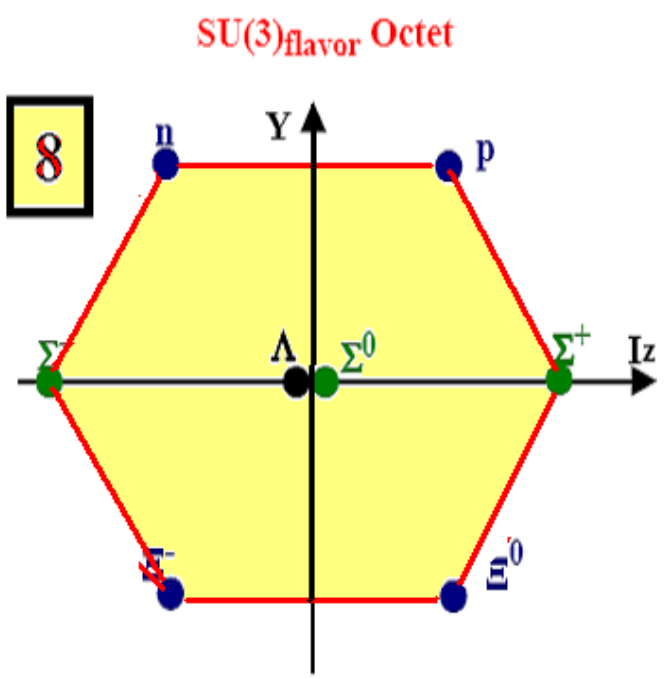
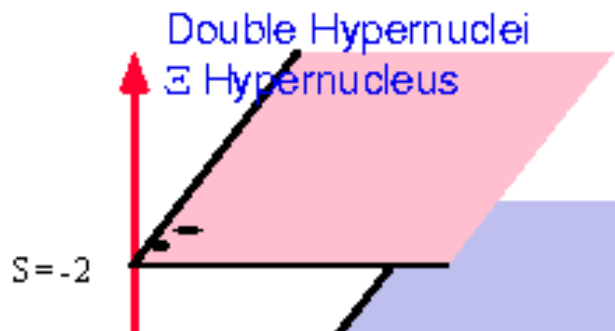
1. Introduction
2. Aspects of  $\Upsilon N$  Interactions
3. Strangeness Production on the Nucleon
4. Strangeness Production by Resonance Excitation
5. Hadro-Production of Hypernuclei
6. Photo- and Electroproduction of Hypernuclei
7. Production of Hypernuclei in Relativistic Fragmentation Reactions
8. Outlook

# I. Introduction




# Strangeness and Hypernuclear Physics: From $SU(2)$ Isospin to $SU(3)$ Flavour Dynamics

## Three-Dimensional Nuclear Chart



umber

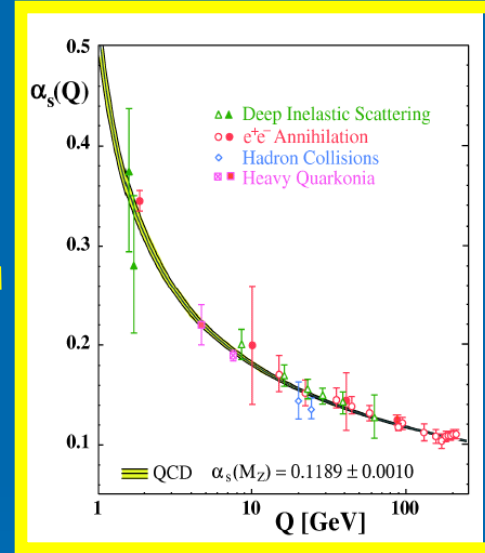
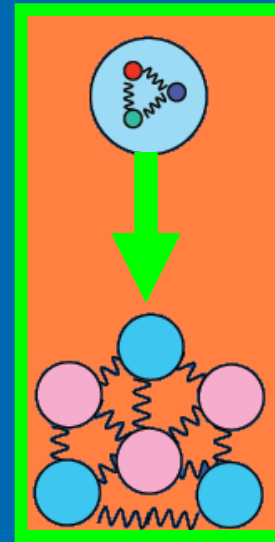
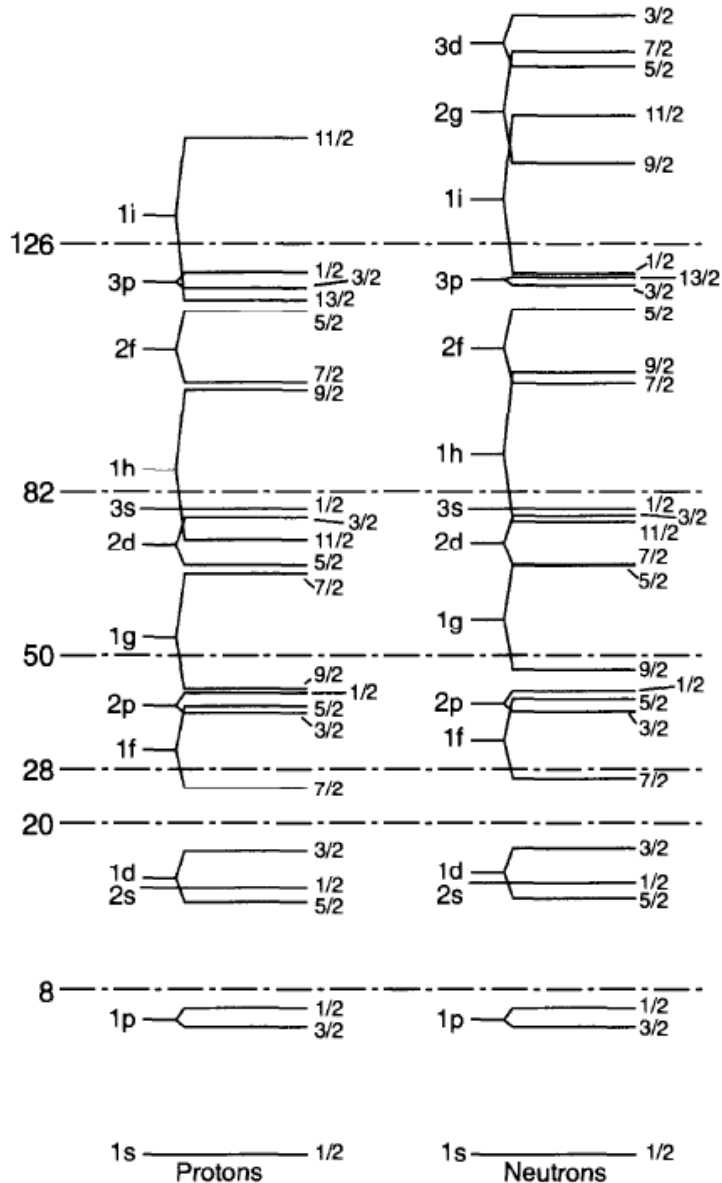
# Hypernuclear Physics and Reaction Studies:

- production mechanism of strangeness
  - reaction dynamics
  - $YN$  and  $YY$  interactions
  - dynamics of nuclear many-body systems with strangeness
  - spectroscopy of hypernuclei
  - which types of hypernuclei do exist?
- 

# Theory of Strong Interactions: QCD

$$\begin{aligned}\mathcal{L}_{\text{QCD}} &= \bar{q} (i\gamma^\mu D_\mu - m) q - \frac{1}{4} F_{\mu\nu}^a F_a^{\mu\nu} \\ &= \bar{q} (i\gamma^\mu \partial_\mu - m) q + g\bar{q}\gamma^\mu T_a q A_\mu^a - \frac{1}{4} F_{\mu\nu}^a F_a^{\mu\nu}\end{aligned}$$

...and from asymptotic freedom...  
to confinement...  
to the **nuclear shell model**

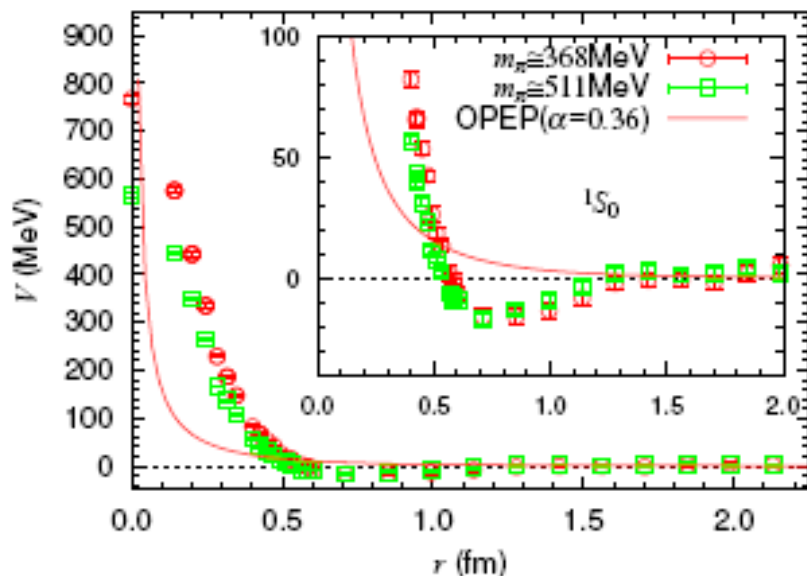


• Nucleus ~ cold, degenerate Fermi-Gas of Quasiparticles

$$U = U_0 + U_{so} \ell \cdot \sigma$$

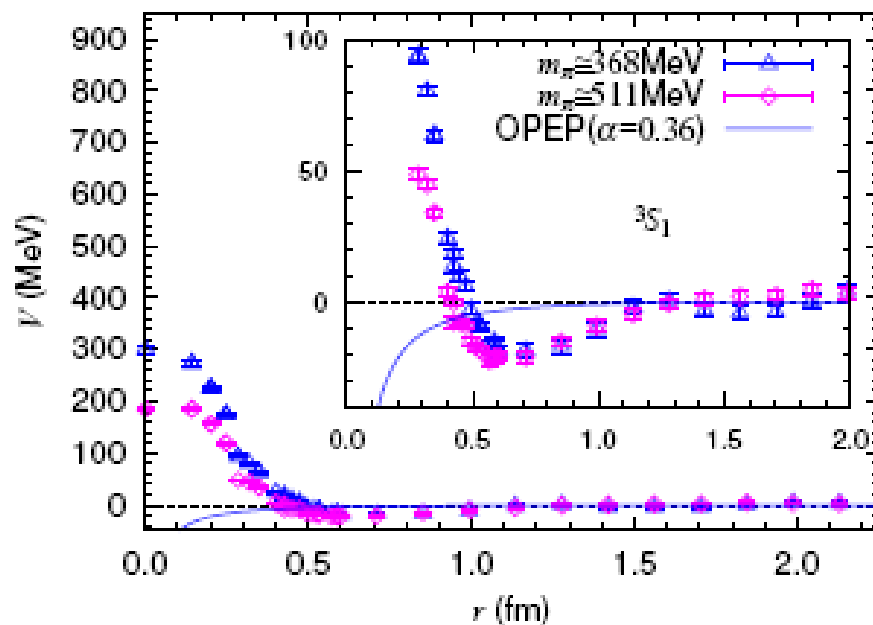
# $p\Xi^0$ ( $S=-2$ ) Potentials from LQCD

„pn“like:  
 $n[udd] \rightarrow \Xi^0[uss]$



$$V_C^\pi = -(1 - 2\alpha) \frac{g_{\pi NN}^2}{4\pi} \frac{(\vec{\tau}_N \cdot \vec{\tau}_\Xi)(\vec{\sigma}_N \cdot \vec{\sigma}_\Xi)}{3} \left( \frac{m_\pi}{2m_N} \right)^2 \frac{e^{-m_\pi r}}{r},$$

[H. Nemura](#), [N. Ishii](#), [S. Aoki](#), [T. Hatsuda](#)  
 arXiv:0806.1094

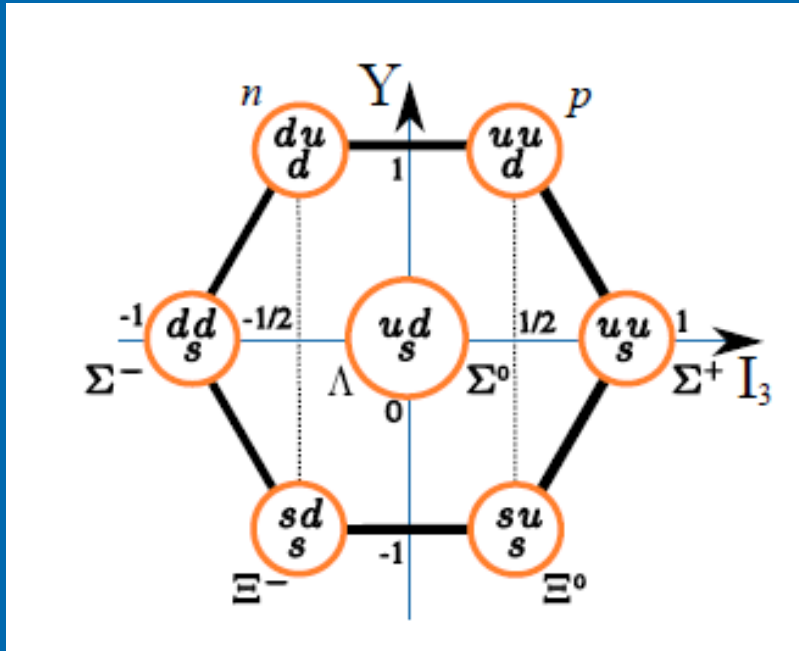




# (Valence) Quark Content of Octet and Decuplet Baryons

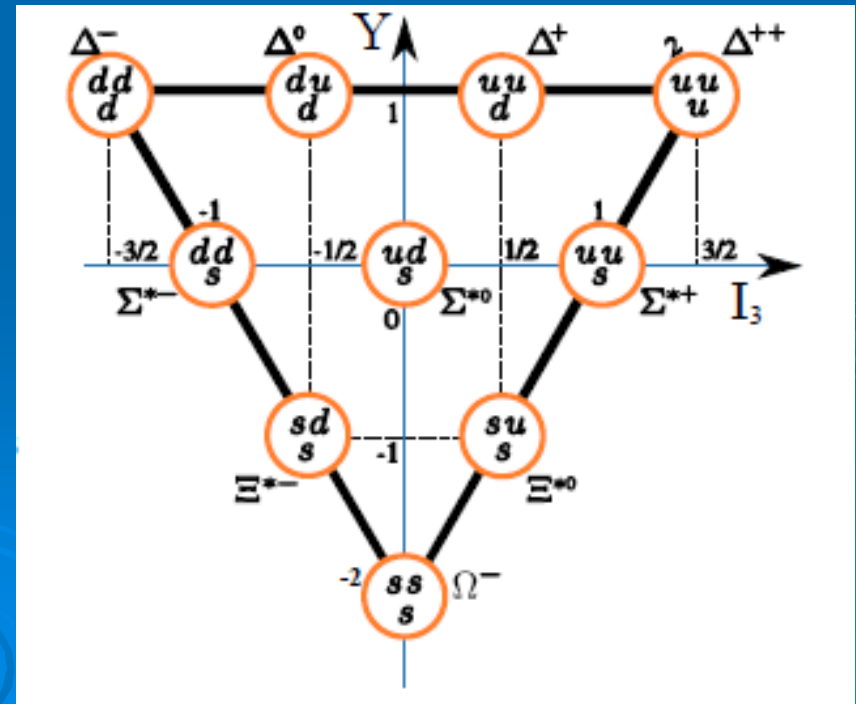
Octet: weak decay of  
hyperons

$$\tau_{1/2} \sim 10^{-8} \dots 10^{-10} \text{ s} \gg \tau_{\text{reac}} \sim 10^{-22} \text{ s}$$



Hypercharge Y and  
Strangeness S:

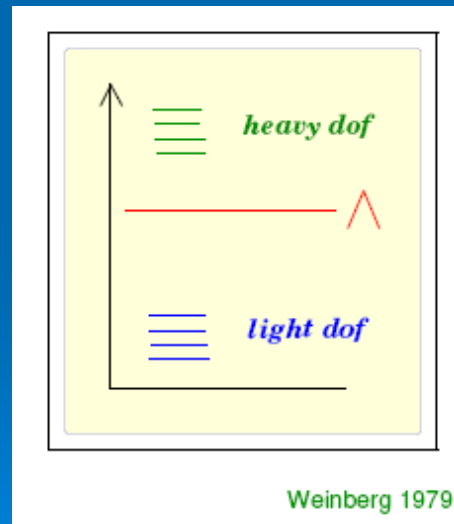
$$Y = S + B = 2(Q - I_3)$$



# QCD and Low-Energy Nuclear Physics:

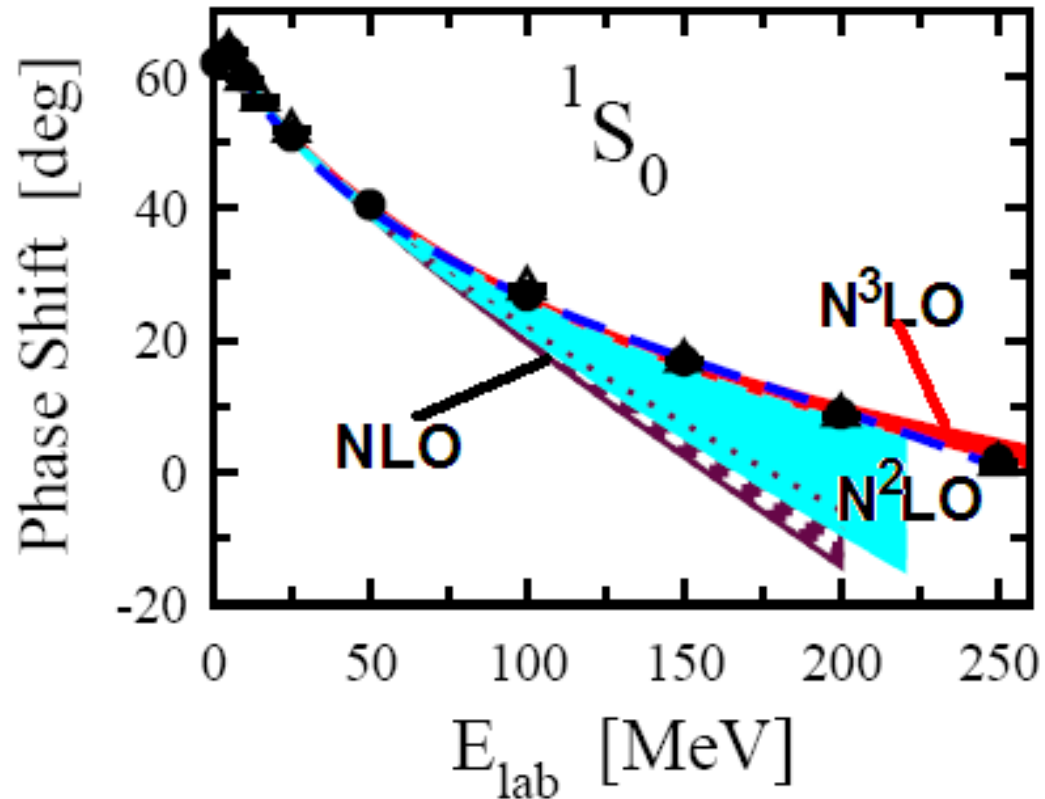
Weinberg Hypothesis (~1979):

- Nuclear Physics  $\cong$  EFT of Pions and Nucleons
- Symmetries of the underlying fundamental theory of QCD
- Spontaneously broken chiral symmetry
- Low energy theorems
- Order-by-Order expansion in  $Q/\Lambda$  with Low Energy Constants (LEC)



$$\mathcal{L}_{\text{QCD}} \rightarrow \mathcal{L}_{\text{EFT}} = \mathcal{L}_{\pi\pi} + \mathcal{L}_{\pi N} + \mathcal{L}_{\text{NN}} + \dots$$

# EFT NN-Phase shifts



$$\mathcal{L}_{\text{QCD}} \rightarrow \mathcal{L}_{\text{EFT}} = \mathcal{L}_{\pi\pi} + \mathcal{L}_{\pi N} + \mathcal{L}_{\text{NN}} + \dots$$

PWA-Data (Symbols): Nijmegen/Virginia Tech

## II. Aspects of YN Interactions



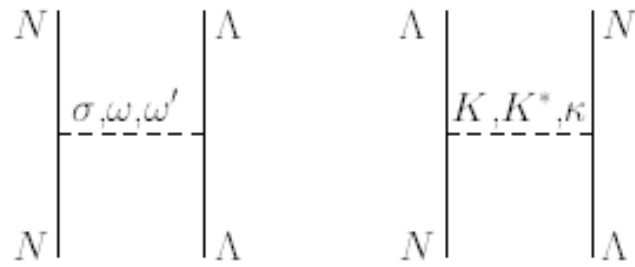
# Some facts about $\Lambda N$ interactions:

1.  $\Lambda N$  interaction is weaker than the nucleon-nucleon interaction,
2.  $\Lambda N$  spin-spin interaction is weak and therefore spin vector  $p_N - h_N$  excitation is suppressed,
3. a  $\Lambda$  hyperon with zero isospin can excite only isoscalar  $p_N - h_N$  modes of the core nucleus,
4. no exchange term with nucleons is required.

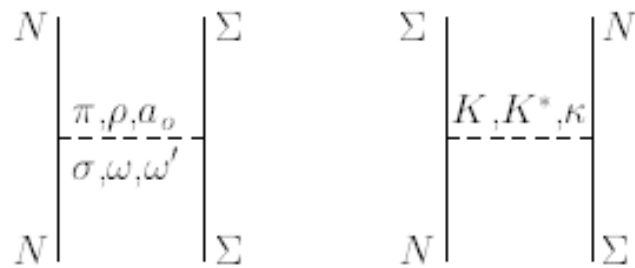
## Non-relativistic empirical form of $\Lambda N$ interactions:

$$V_{\Lambda N}(r) = V_0(r) + V_\sigma(r) \mathbf{s}_\Lambda \mathbf{s}_N + V_A(r) \mathbf{l}_{\Lambda N} \mathbf{s}_\Lambda + V_N(r) \mathbf{l}_{\Lambda N} \mathbf{s}_N + V_T(r) S_{12}$$

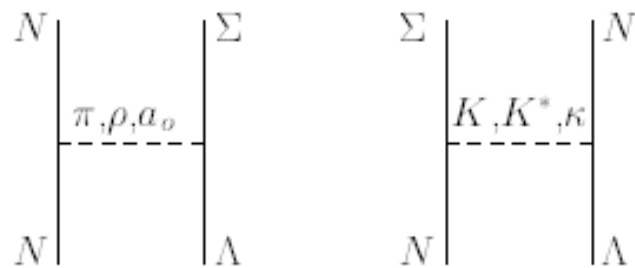
# Meson-exchange picture for $YN$ interactions



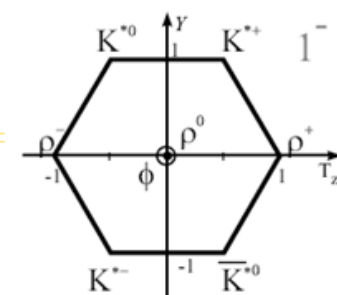
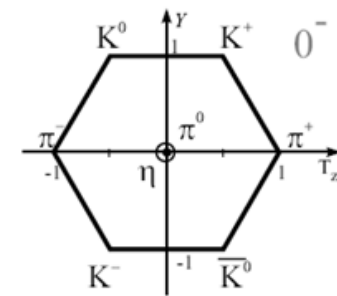
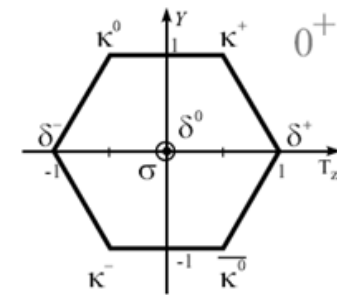
(a)



(b)

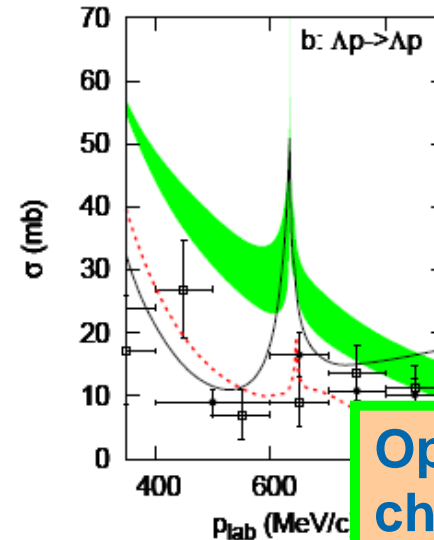
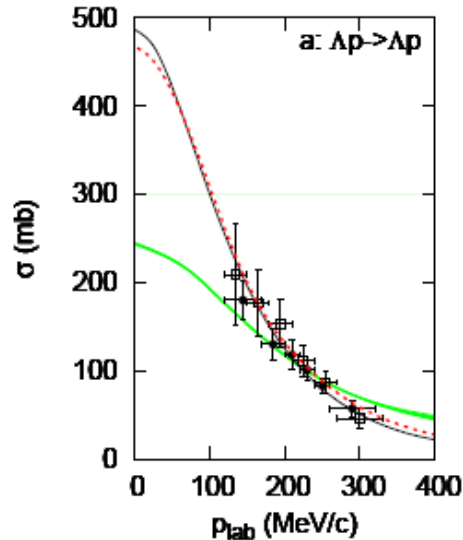


(c)

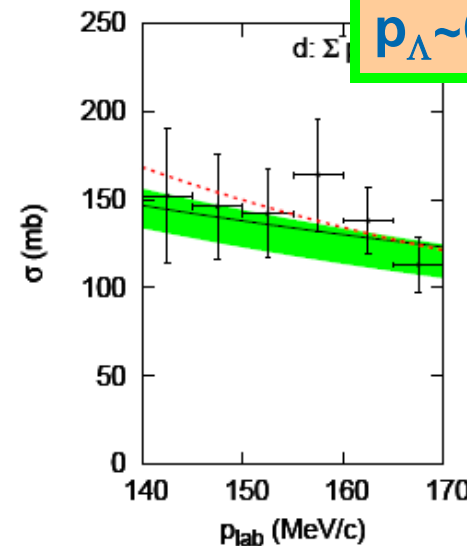
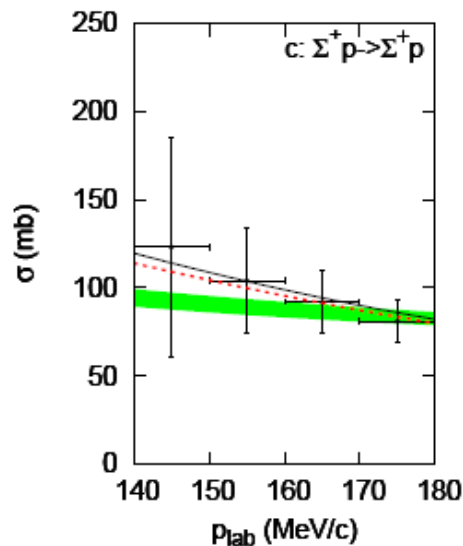


# OBE and $\chi$ EFT NY-Cross Sections:

Results by the  
Jülich Group:  
E. Epelbaum et  
al.

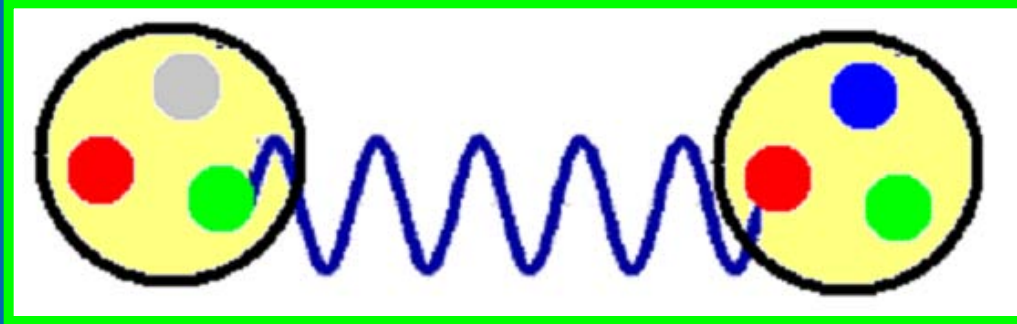


Opening of the  $\Sigma N$   
channel at  
 $p_{\Lambda} \sim 650 \text{ MeV/c}$



- $\chi$ EFT (LO)
- Jülich 04
- Nijmegen SC97

# Scaling of (In-Medium) Hyperon Interactions



Naïve Quark Model Scaling:

$$g_{m\Lambda} = \frac{2}{3} g_{mN} \dots$$

or  $SU(3)/SU(6)$  relations...

but...

$$K_{\Lambda N} = \frac{1}{1 - z V_{NN} G_{QF}} \cdot z V_{NN} = \mathbf{R} K_{NN}$$

$$\mathbf{R}_m = \frac{g_{mNY}}{g_{mNN}} (1 + \chi_m(k_F, \Delta M)(1 - z_m) \dots)$$



# ...characterizing interactions by their strength: s-wave Effective Range Expansion

$$\frac{\tan(\delta)}{q_s} = -\frac{2\mu}{(\hbar c)^2 4\pi} K(q_s, q_s)$$

$$\frac{1}{\mu} = \frac{1}{M_1} + \frac{1}{M_2}$$

$$\frac{q_s}{\tan(\delta)} = -\frac{1}{a} + \frac{1}{2} q_s^2 r + \dots$$

- scattering length  $a$
- effective range  $r$

# ...scaling for free space $N\Lambda$ Interactions?

$$a_s^{N\Lambda} = -1.8_{-4.2}^{+2.3} \text{ fm}$$

$$a_t^{N\Lambda} = -1.8_{-0.8}^{+1.1} \text{ fm}$$

$$a_s^{np} = -23.751 \text{ fm}$$

$$a_t^{np} = +5.423 \text{ fm}$$

$$\mathbf{K}_{N\Lambda} = \mathbf{K}_{00} + \mathbf{K}_{10} \vec{\sigma}_N \cdot \vec{\sigma}_\Lambda + \dots$$

$$a_s^{N\Lambda} \sim \mathbf{K}_s = \mathbf{K}_{00} - 3\mathbf{K}_{10} \sim \mathbf{K}_\sigma + \mathbf{K}_\omega - 3\mathbf{K}_\eta$$

$$a_t^{N\Lambda} \sim \mathbf{K}_t = \mathbf{K}_{00} + \mathbf{K}_{10} \sim \mathbf{K}_\sigma + \mathbf{K}_\omega + \mathbf{K}_\eta$$

→ Scaling Factors  $R_m = \mathbf{K}_{mN\Lambda} / \mathbf{K}_{mNN} \sim 1/40 \dots 1/4$

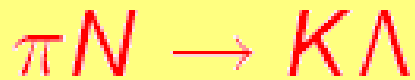
( $m = \sigma, \omega, \eta$ )

# IV. Strangeness Production on the Nucleon

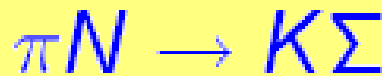
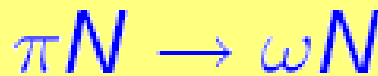
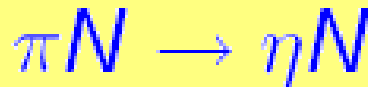
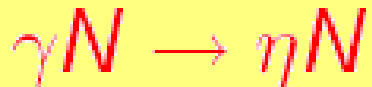
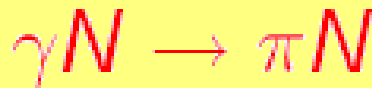
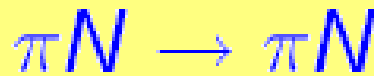
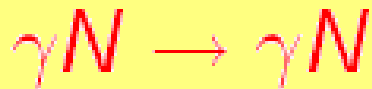


# The Giessen Model: Coupled Channels Approach to Meson Production on the Nucleon below 2GeV

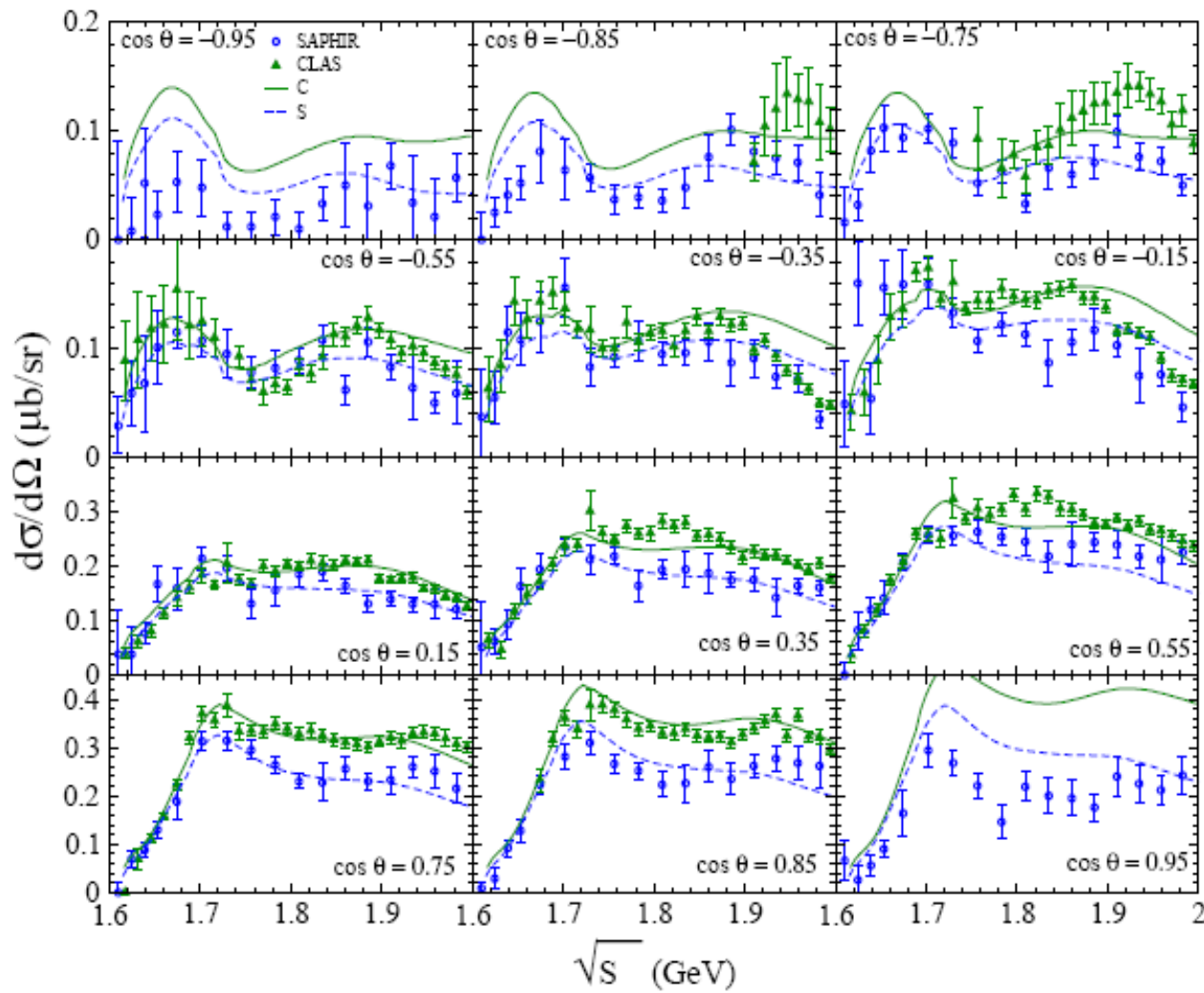
$$T_{ab}(q, q') = V_{ab}(q, q') + \sum_c \int \frac{d^3k}{(2\pi)^3} V_{ac}(q, k) G_{cc}(k, q_s) T_{cb}(k, q')$$



+



# $\gamma p \rightarrow K\Lambda$ Results from the Giessen Model

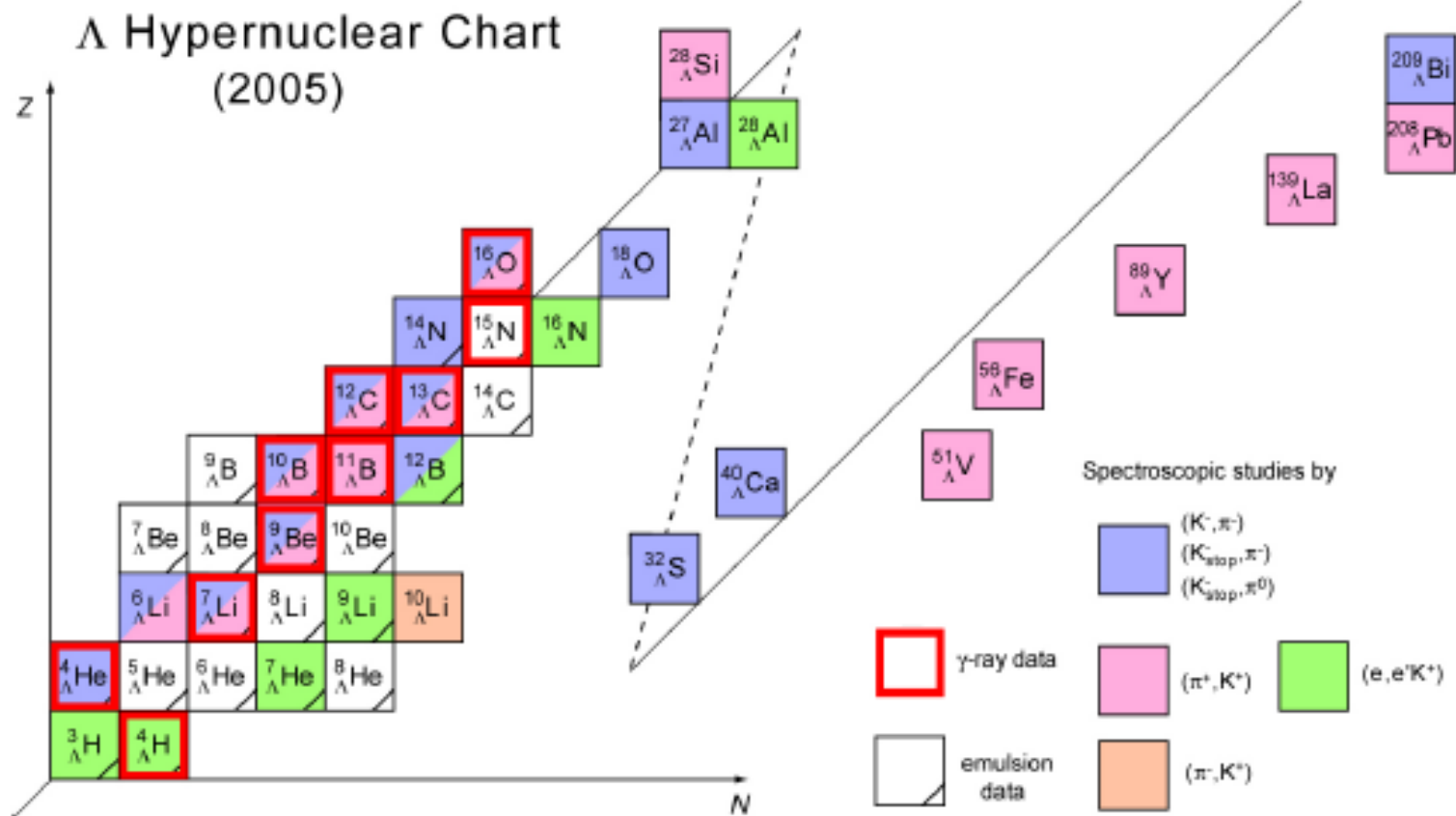


- separate fits to **SAPHIR** and **CLAS** data
- constraints from other hadronic and  $\gamma$  channels

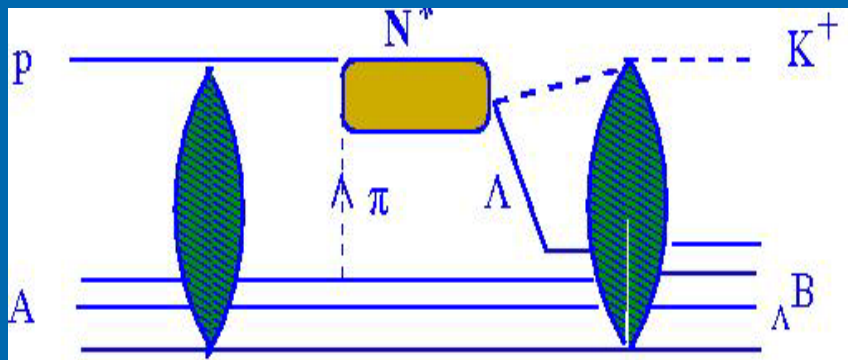
# IV. Production of Hypernuclei: The Giessen Resonance Model



# 4.1 Known $\Lambda$ -Hypernuclei and Spectroscopic Studies

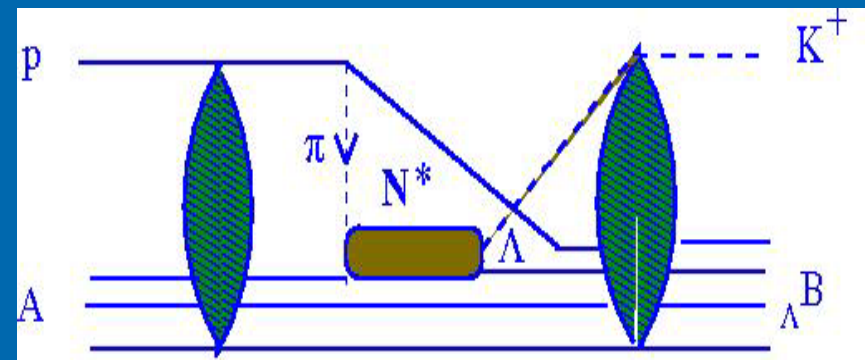


## 4.2 Dynamics of strangeness production: The Giessen Resonance Model



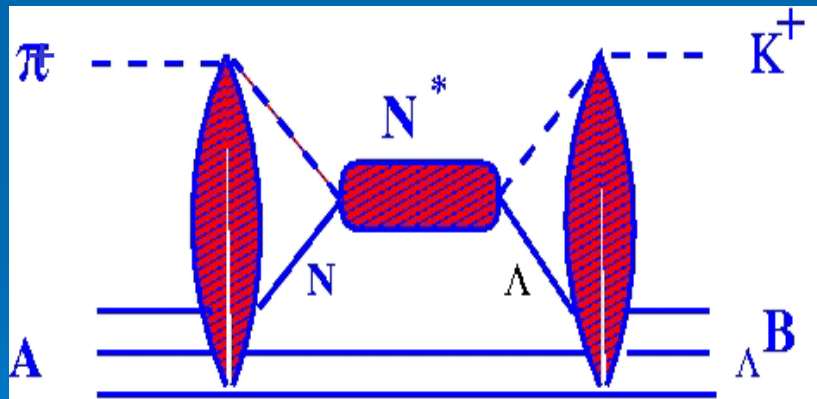
Target emission

$A(p, K^+)_{\Lambda} B$

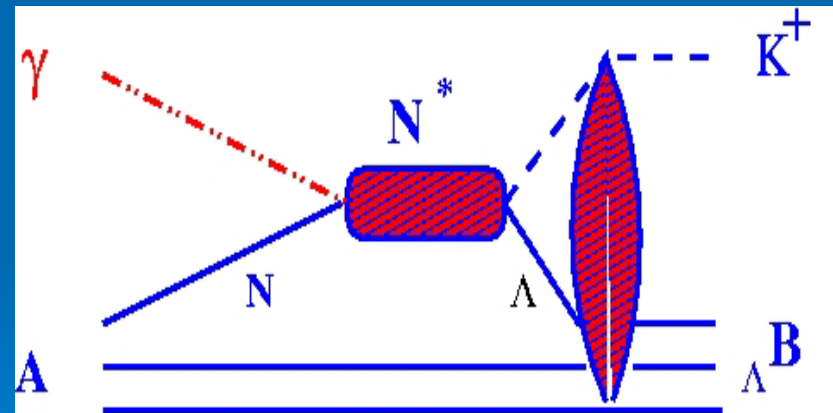


Projectile emission

$A(p, K^+)_{\Lambda} B$



$A(\pi^+, K^+)_{\Lambda} B^*$



$A(\gamma, K^+)_{\Lambda} B'$

$N^*(1650)$ ,  $N^*(1710)$ ,  $N^*(1720)$  resonances (PDG).



...we need:

- dynamics of the particles used as probes
- description of the production dynamics
- dynamics of the hyperon in nuclear matter

